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Indian Standard

CODE OF PRACTICE FOR
DESIGN IN TUNNELS CONVEYING WATER

PART IV STRUCTURAL DESIGN OF CONCRETE LINING IN ROCK

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CODE OF PRACTICE FOR
DESIGN OF TUNNELS CONVEYING WATER

PART IV STRUCTURAL DESIGN OF CONCRETE LINING IN ROCK

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AMENDMENT NO. 1 JUNE 1986

TO

IS:4680(Part 4)-1971 CODE OF PRACTICE FOR DESIGN OF TUNNELS CONVEYING WATER

PART 4 STRUCTURAL DESIGN OF CONCRETE LINING IN ROCK

(Page 24, clause D-2.1, line 7) - Substitute the following for the existing line:

\( m_1, m_2 = \) Poisson's number of rock and concrete respectively.

(Page 24, clause D-2.1, lines 13 and 14) - Substitute the following in the existing lines:

\( a = \) internal radius of the tunnel; and
\( b = \) external radius of the lining up to A-line.

(BDC 58)
AMENDMENT NO. 2 JANUARY 2008 TO
IS 4880 (PART 4) : 1971 CODE OF PRACTICE FOR DESIGN IN TUNNELS CONVEYING WATER

PART 4 STRUCTURAL DESIGN OF CONCRETE LINING IN ROCK

(Page 5, clause 3.1) — Substitute ‘IS 456 : 2000*’ for ‘IS 456 : 1964*’.

(Page 9, clause 6.1) — Substitute ‘IS 456 : 2000*’ for ‘IS 456 : 1964*’.

(Pages 5 and 9, footnote marked *) — Substitute the following for the existing footnote:

‘Plain and reinforced concrete — Code of practice (fourth revision)’
Indian Standard

CODE OF PRACTICE FOR
DESIGN OF TUNNELS CONVEYING WATER

PART IV STRUCTURAL DESIGN OF CONCRETE LINING IN ROCK

0. FOREWORD

0.1 This Indian Standard (Part IV) was adopted by the Indian Standards Institution on 15 March 1971, after the draft finalized by the Water Conductor Systems Sectional Committee had been approved by the Civil Engineering Division Council.

0.2 Water conductor system occasionally takes the form of tunnels through high ground or mountains, in rugged terrain where the cost of surface pipe line or canal is excessive and elsewhere as convenience and economy dictates. This standard, which is being published in parts, is intended to help engineers in design of tunnels conveying water. This part lays down the criteria for structural design of concrete lining for tunnels in rock, covering recommended methods of design. However, in view of the complex nature of the subject, it is not possible to cover each and every possible situation in the standard and many times a departure from the practices recommended in this standard may be considered necessary to meet the requirements of a project or site for which discretion of the designer would be required.

0.3 This standard is one of a series of Indian Standards on tunnels. (see page 28).

0.4 Other parts of this standard are as follows:
   Part I General design
   Part II Geometric design
   Part III Hydraulic design
   Part IV Structural design of concrete lining in rock
   Part V Structural design of concrete lining in soft strata and soils
   Part VI Tunnel supports

0.5 For the purpose of deciding whether a particular requirement of this standard is complied with, the final value, observed or calculated, expressing the result of a test or analysis, shall be rounded off in accordance with IS: 2-1960*. The number of significant places retained in the rounded off value should be the same as that of the specified value in this standard.

*Rules for rounding off numerical values (revised).
1. SCOPE

1.1 This standard (Part IV) covers criteria for structural design of plain and reinforced concrete lining for tunnels and circular shafts in rock mainly for river valley projects.

Note — The provisions may, nevertheless, be used for design of any other type of tunnel, like railway or roadway tunnel, provided that all the factors peculiar to such projects which may affect the design are taken into account.

1.2 This standard, however, does not cover the design of steel and prestressed concrete linings, tunnels in swelling and/or squeezing type of rocks, soils or clays and cut and cover sections.

2. TERMINOLOGY

2.0 For the purpose of this standard, the following definitions shall apply.

2.1 Minimum Excavation Line (A-Line) — A line within which no unexcavated material of any kind and no supports other than permanent structural steel supports shall be permitted to remain (see Fig. 1).
2.2 Pay Line (B-Line) — An assumed line (beyond A-line) denoting mean line to which payment of excavation and concrete lining is made whether the actual excavation falls inside or outside it.

2.3 Cover — Cover on a tunnel in any direction is the distance from the tunnel soffit to the rock surface in that direction. However, where the thickness of the overburden is sizable its equivalent weight may also be reckoned provided that the rock cover is more than three times the diameter of the tunnel.

3. MATERIAL

3.1 Use of plain and reinforced concrete shall generally conform to IS:456-1964.

4. GENERAL

4.1 Structural design of tunnel lining requires a thorough study of the geology of rock mass, the effective cover, results of in situ tests for modulus of elasticity, poisson's ratio, state of stress and other mechanical characteristics of the rock. It is preferable to make a critical study of these factors which may be done in pilot tunnels, test drifts, during actual excavations or by other exploratory techniques. The assessment of rock load on the lining and portion of the internal pressure which should be assumed to be transmitted to the rock mass, will have to be done by the designer on the basis of the results of these investigations.

4.2 It is essential for the designer to have fairly accurate idea of the seepage, and the presence or absence of ground water under pressure likely to be met with. Where heavy seepage of water is anticipated, the designer shall make provisions for grouting with cement and/or chemicals or extra drainage holes, and also consider the feasibility of providing steel lining, if necessary. It is recommended that such designs of alternate use of steel lining be made along with the design of plain or reinforced lining so that a design is readily available should the construction personnel require it when they meet unanticipated conditions.

4.3 The portions of a tunnel which should be reinforced and the amount of reinforcement required depends on the physical features of the tunnel, geological factors and internal water pressure. For a free-flow tunnel normally no reinforcement need be provided. However, reinforcement shall be provided where required to resist external loads due to unstable ground or grout or water pressures. Pressure tunnels with high hydrostatic loads shall have lining reinforced sufficiently to withstand bursting where inadequate cover or unstable supporting rock exists.

*Code of practice for plain and reinforced concrete (second revision).*
4.3.1 The provision of reinforcement in the tunnel lining complicates the construction sequence besides requiring a thicker lining. The use of reinforcement should, therefore, be restricted, as much as possible consistent with the safety of lining. For free flow tunnels it is recommended that as far as possible, no reinforcement should be provided to resist external loads. Such loads should be resisted and taken care of by steel supports and/or precast concrete rings.

4.3.2 A pressure tunnel should ordinarily be reinforced wherever the depth of cover is less than the internal pressure head. The final choice whether reinforcement should be provided or not would be guided by the geological setup and economics.

4.3.3 For design of junctions and transitions for tunnels detailed structural analysis shall be made. Such transitions are difficult to construct in the restricted working space in tunnels, and the designer shall keep in view this aspect and propose structures which are easy for construction.

4.3.4 An adequate amount of both longitudinal and circumferential reinforcement in addition to steel supports may be provided, if required, near the portals of both pressure and free-flow tunnels to resist loads resulting from loosened rock headings or from sloughing of the portal cuts.

4.4 If the seepage of water through the lining is likely to involve heavy loss of water and the structural stability of the rock mass around the tunnel is likely to be affected adversely or might lead to such situation as to be damaging to the tunnel or adjoining structures, steel lining shall be provided. Where rock cover is less than that specified in 4.5 and 4.5.1 or where the cavitation of lining is expected due to the high velocity of water or erosion is expected the provision of a steel liner shall be considered.

4.5 Where the rock is relatively impervious and the danger of blowout exists, the vertical cover shall be greater than the internal pressure head in the tunnel. In other cases the weight of the rock over the tunnel shall be greater than the internal pressure.

Note — The conventional practice is to provide a vertical cover equal to the internal water pressure head (H). Recent trend, however, is to provide lesser cover (as low as 0.5 H) depending upon the nature of the rock.

4.5.1 For tunnels located near mountain slopes, the lateral cover rather than the vertical cover may be the governing criteria many times. In such cases the effective vertical cover equivalent to the actual lateral cover shall be found out, by drawing a profile of the ground surface (perpendicular to the contour lines) and fitting the curve shown in Fig. 2 in such a way that it touches the ground surface. The vertical distance
marked \( C_e \) shall be designated as the effective vertical cover and shall be greater than the internal pressure head in the tunnel. This method of estimating the effective cover shall not hold good where joints, stratification, faults, etc., in the rock are adversely located to invalidate the assumption that horizontal cover is half as effective as the vertical cover on the basis of which the curve of Fig. 2 is drawn. In such cases special analysis shall be made for determining the stability of the rock mass around the tunnel.

\[ \alpha = 26^\circ 23' 16'' \]

\[ \text{VERTICAL COVER GOVERS} \]

\[ \text{HORIZONTAL COVER GOVERS} \]

\[ \text{DIAGONAL COVER GOVERS} \]

**Fig. 2 Estimation of Effective Cover**

5. **Loading Conditions**

5.1 **General** — Design shall be based on the most adverse combination of probable load conditions, but shall include only those loads which have reasonable probability of simultaneous occurrence.

5.2 **Load Conditions** — The design loading applicable to tunnel linings shall be classified as 'Normal' and 'Extreme' design loading conditions. Design shall be made for 'Normal' loading conditions and shall be checked
for safety under ‘Extreme’ loading conditions (see Appendix A). The design loading shall be as follows:

a) **External Rock Load** (see 7.4.2)

b) **Self Load of Lining**

c) **Design External Water Pressure** (see 7.4.3):

1) **Normal design loading conditions** — The maximum loading obtained from either maximum steady or steady state condition with loading equal to normal maximum ground water pressure and no internal pressure, or maximum difference in levels between hydraulic gradient in the tunnel, under steady state or static conditions and the maximum down surge under normal transient operation.

2) **Extreme design loading conditions** — Loading equal to the maximum difference in levels between the hydraulic gradient in the tunnel under static conditions and the maximum down surge under extreme transient operations or the difference between the hydraulic gradient and the tunnel invert level in case of tunnel empty condition.

d) **Design Internal Water Pressure**:

1) **Normal design loading conditions** — Maximum static conditions corresponding to maximum water level in the head pond, or loading equal to the difference in levels between the maximum upsurge occurring under normal transient operation and the tunnel invert.

2) **Extreme design loading conditions** — Loading equal to the difference between the highest level of hydraulic gradient in the tunnel under emergency transient operation and the invert of the tunnel.

e) **Grout Pressures** (see 7.4.4)

f) **Other Loads** — Pressure transmitted from buildings and structures on external surface lying within the area of subsidence and non-permanent loads, such as weight of vehicles moving in the tunnel or on the surface above it, where applicable.

5.3 The loading conditions vary from construction stage to operation stage and from operation stage to maintenance stage. The design shall be checked for all probable combination of loading conditions likely to occur during all these stages.
6. STRESSES

6.1 For design of concrete lining, the thickness of concrete up to A-line shall be considered. The stresses for concrete and reinforcement shall be in accordance with IS: 456-1964* for design of lining for condition of normal load.

6.1.1 For extreme conditions of loading, the stresses in accordance with 6.1 shall be increased by 33\(\frac{1}{3}\) percent.

7. DESIGN

7.1 The design of concrete lining for external loads may be done by considering it as an independent structural member (see 7.4). The design of concrete lining for internal water pressure may be done by considering the lining as a part of composite thick cylinder consisting of peripheral concrete and surrounding rock mass subjected to specific boundary conditions (see 7.5).

**NOTE** — To ensure the validity of the assumption that lining is a part of composite thick cylinder in the latter case adequate measures shall be taken, such as pressure grouting of the rock mass surrounding the tunnel.

7.2 **Thickness of Lining** — The thickness of the lining shall be designed such that the stresses in it are within permissible limits when the most adverse load conditions occur. The minimum thickness of the lining will, however, be governed by requirements of construction. It is recommended that the minimum thickness of unreinforced concrete lining be 15 cm for manual placement. Where mechanical placement is contemplated the thickness of the lining shall be so designed that the slick line can be easily introduced on the top of the shutter without being obstructed by steel supports. For a 15-mm slick line a clear space of 18 cm is recommended. For reinforced concrete lining, a minimum thickness of 30 cm is recommended, the reinforcement, however, being arranged in the crown to allow for proper placement of slick line.

7.2.1 However, for preliminary design of lining for tunnels in reasonably stable rock, a thickness of lining may be assumed to be 6 cm per metre of finished diameter of tunnel.

**NOTE** — Minimum thickness of lining, as necessary from structural considerations, should be provided since thin linings are more flexible and shed off loads to the abutments.

7.3 Where structural steel supports are used, they shall be considered as reinforcement only if it is possible to make them effective as reinforcement by use of high tensile bolts at the joints or by welding the joints. A

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*Code of practice for plain and reinforced concrete (second revision).
minimum cover of 15 cm shall be provided over the inner flange of steel supports and a minimum cover of 8 cm over the reinforcement bars.

Note — Welding of joints in soft strata tunnels may not be possible, and it may become necessary to embed the steel supports partly or fully in primary concrete immediately after erection. Welded joints should, therefore, be avoided.

7.4 Design for External Loads — The lining may be considered as an independent structural element assuming that it deflects under the active external loads and its deflection is restricted by the passive resistance developed in the surrounding rock mass. At any point on the periphery of the lining this may be stated by the following equation:

\[ \Delta \rho = \Delta r + \Delta e + \Delta w - \Delta y \]

where

- \( \Delta \rho \) = deflection due to passive resistance;
- \( \Delta r \) = deflection due to rock load;
- \( \Delta e \) = deflection due to self weight of lining and the water contained in it;
- \( \Delta w \) = deflection due to the external water pressure, if any; and
- \( \Delta y \) = yield of surrounding rock mass due to abutting of the lining against it.

7.4.1 The following loads and reactions are involved in the design of lining:

a) Rock load (see 7.4.2);
b) External pressure of water, if any (see 7.4.3);
c) Grout pressure, if any (see 7.4.4);
d) Self weight of lining;
e) Weight of water contained in the tunnel;
f) Reaction due to active vertical loads (see 7.4.5); and
g) Lateral passive pressure due to the deformation of lining (see 7.4.6).

Note — As compared to the other loads, the self weight and the weight of water contained in the tunnel are small. These loads are not discussed in detail. However, the formulae for calculating bending moment, thrust, radial shear and horizontal and vertical deflections caused by self load and the weight of water contained in the conduit are given in Appendix C.

7.4.2 Rock Load — Rock load acting on the tunnel varies depending upon the type and mechanical characteristics of rock mass pre-existing stresses in the rock mass and the width of the excavation. The rock load is also affected by ground water conditions which may lubricate the joints in rock and cause greater load than when the material is dry.
The existing stresses and their distribution after tunnelling has a great effect on the development of load on tunnel lining. The redistribution may take considerable time to reach an equilibrium condition. Wherever it is felt that rock loads are likely to develop excessively it is advisable to prevent the movement of rock by immediately supporting it by shotcreting and/or steel supports and primary lining. Where weak rocks are supported by steel rib supports, much of the rock load would be taken by the supports and the lining would take the load developed after its placement. There may also be redistribution of stresses in supports due to deformation of the lining. A reasonable approach is to determine the diametral changes in the supported section with respect to time before concreting to estimate the extent of deformation that has already taken place. This investigation may be conveniently done in an experimental section of the tunnel or pilot tunnel with proper instrumentation.

In major tunnels, it is recommended that as excavation proceeds load cell measurements and diametral change measurements are carried out to estimate the rock loads. In rocks where the loads and deformations do not attain stable values, it is recommended that pressure measurements should be made using flat jack or pressure cells.

7.4.2.1 In the absence of any data and investigations, rock loads may be assumed to be acting uniformly over the tunnel crown as shown in Fig. 3 in accordance with Appendix B. However, Appendix B may be taken as an aid to judgement by the designer.

![Diagram showing external loads on lining](image)

**FIG. 3 EXTERNAL LOADS ON LINING**

**7.4.3 External Water Pressure** — Lining shall be designed for external water pressure, if any. However, in areas where drainage holes are provided, lining shall not be designed for external water pressure (see 8.1). For
conditions of loading for external water pressure reference may be made to 5.2. For design of lining for external water pressure where effective pressure grouting has been done, the water pressure may be assumed to act on the whole grouted cylinder which may be taken as a structural element for computing the stresses and deformation of lining.

7.4.4 Grout Pressures — The lining shall be checked for stresses developed in it at the pressure on which grouting is done and it shall be ensured that the stresses are within the limits depending on the strength attained by concrete by then (see 9.1 and 9.2).

7.4.5 Vertical Reactions — Reactions due to the vertical loads may be assumed, reasonably, to be vertical and uniformly distributed on the invert of the lining as shown in Fig. 3.

**Note** — In fact, these reactions may, however, not be uniform depending upon the foundation conditions. Nevertheless, with the uncertainties involved in the design of tunnels, the assumption may not give far out results. Moreover, normally, uniform reactions would give more critical condition.

7.4.6 Lateral Passive Pressure — The lateral passive pressure may be estimated either by considering the lining as a ring restrained by elastic medium with a suitable modulus of deformation or by restricting the maximum deflection of the lining at the horizontal diameter to an assumed value (depending upon the yield of the surrounding rock mass) by the lateral passive pressure. The latter method is discussed in detail in 7.4.6.1 for design of circular linings. For design of non-circular linings the former method shall only be used.

7.4.6.1 For analyzing a circular lining, the designer will have to assume the maximum deflection to be permitted along the horizontal central axis of the tunnel. This value of horizontal deflection will consist of the yield of the rock mass surrounding the tunnel (see Note 2). It may be assumed that any further deflection of the lining is restricted to this value by the lateral passive resistance of the surrounding rock mass in a pattern given in Fig. 3. The design shall be such that the maximum value of the passive resistance is within the maximum permissible values.

**Note** 1 — For a circular lining the deflection is outward in a zone extending approximately from 45° above the horizontal diameter to the invert as the invert move up. The maximum value is near horizontal diameter. On the above consideration and neglecting the effect of vertical translation of the lining, the lateral rock restraint may be assumed to have approximately a triangular distribution as shown in Fig. 3. The vertical translation of the lining would cause a shifting of the point of maximum intensity slightly below the horizontal diameter and restriction of the upper limit to an angle slightly less than 45°, but the effect of vertical translation would be small and can be neglected. The passive pressures would, in fact, be also radial to the surface but in view of the fact that the deflections would be mostly in horizontal direction and vertical deflections would be small, it may be assumed to act in horizontal direction.
NOTE 2 — The rock mass surrounding the tunnel yields due to the bearing pressure of lining against it. This yield may be due to closing up of joints and fractures in the rock mass and also due to its elastic or plastic deformation. The value of yield taken for design should be based on the experiments carried out in the test sections (see 4.1).

At Bhakra Dam, rock deflection tests indicated yield of either face in poor shattered rock as 1.25 mm under a stress of 54 kg/cm². However, a total deflection of 3.8 mm was assumed in the design of lining though actual bearing pressure on the rock was anticipated to be much less. Experiments on Garrison Dam tunnels, in clay shale of internal diameter 8.8 m and lining thickness of 0.9 m indicated deflection of either face of lining at horizontal diameter to range between 3 to 4 mm. In design of Ramganga Dam tunnels outer deflection of either face of lining at horizontal diameter was assumed to be 3.8 mm.

7.4.6.2 Formulae for determining the values of horizontal deflection, vertical deflection, bending moments, normal thrust, radial shear for the various circumferential points on a circular lining are given in Appendix C considering the invert as the reference point for various loads excepting the internal pressure. In derivation of these values the pattern of vertical reaction and passive pressure has been assumed in accordance with 7.4.5 and 7.4.6 as shown in Fig. 3.

7.4.7 For non-circular lining model tests are recommended to determine the stress distributions. However, the design may be done assuming uniformly distributed loads as in the case of circular tunnels, and using the same distribution for passive pressures. The design of such indeterminate sections may be done by standard methods and is not covered by this standard.

7.5 Design For Internal Water Pressure — Lining shall be considered as a part of composite thick cylinder consisting of peripheral concrete and surrounding rock mass subjected to specified boundary conditions.

NOTE — This method suffers from uncertainties of external loads, material properties and indeterminate tectonic forces. In this method the rock surrounding the tunnel is assumed to have reasonably uniform characteristics and strength and that effective pressure grouting has been done to validate the assumption that concrete lining and surrounding rock behave as a composite cylinder. The grout fills the cracks in the rock and thus reduces its ability to deform inelastically and increases the modulus of deformation. If the grout pressures are high enough to cause sufficient prestress in the lining the effect of temperature and drying shrinkage and inelastic deformation might be completely counteracted.

7.5.1 For analysing a circular lining the method given in Appendix D may be adopted. The design shall be such that at no point in the lining and the surrounding rock the stresses exceed the permissible limits.

If the rock is very good, and cracking of lining is not otherwise harmful, cracking of the lining may be permitted to some extent. In that case, tangential stress in concrete lining will be absent and correspondingly, tangential stress in rock will increase.
If the rock is not good, tensile stress in concrete may exceed the allowable limit and in such a case, reinforcement may be provided. Reinforcement however, is not capable of reducing the tensile stresses to a considerable extent. By suitable arrangement, it will help to distribute the cracks on the whole periphery in the form of hair cracks which are not harmful because they may get closed in course of time, or at least they will not result in serious leakages.

7.5.2 For analyzing non-circular linings, the stress pattern may be determined by photo-elastic studies.

8. GROUND WATER DRAINAGE HOLES

8.1 Drainage holes may be provided in other than water conveying tunnels to relieve external pressure, if any, caused by seepage along the outside of the tunnel lining. In free flow tunnels drainage holes may be provided in the crown above the full supply level. In case of pressure tunnels, if the external water pressure is substantially more than the internal water pressure, drainage holes may be provided in the crown. However, when the mountain material is likely to be washed into the tunnel through such drainage holes they shall not be provided.

8.1.1 The arrangement of drainage holes depends upon the site conditions and shall be decided by the designer. A recommended arrangement is described below:

At successive sections: one vertical hole drilled in the crown alternating with two drilled horizontal holes one in each side wall extending to a depth of at least 15 cm beyond the back of the lining.

8.1.2 If the flow through the tunnel is conveyed in a separate pipe, the horizontal holes shall be drilled near the invert.

9. GROUTING

9.1 Backfill Grouting — Backfill grouting shall be done at a pressure not exceeding 5 kg/cm² and shall be considered as a part of concreting. It shall be done throughout the length of the concrete lining not earlier than 21 days after placement after the concrete in the lining has cooled off. However, stresses developed in concrete at the specified grout pressure may be calculated and seen whether they are within permissible limits depending on the strength attained by concrete by then. The grout pressure mentioned above is the pressure as measured at the grout hole.

Note — Backfill grouting serves to fill all voids and cavities between concrete lining and rock.

9.2 Pressure Grouting — Pressure grouting shall be done at a maximum practicable pressure consistent with the strength of lining and safety against uplift of overburden. The depth of grout holes shall be at least equal to the diameter of the tunnel.

Note 1 — Pressure grouting consolidates the surrounding rock and fills any gaps caused by shrinkages of concrete. This grouting is normally specified where lining is
reinforced, to improve the rock quality and, therefore, to increase the resistance of rock to carry internal water pressure. As a rule of thumb a grout pressure of 1.5 times the water pressure in the tunnel may be used subject to the conditions that safety against uplift of the overburden is ensured. Grout pressures of up to 5 to 10 times the water pressure in the tunnel have been used in Italy.

**NOTE 2** — It is advantageous to provide a grout curtain by means of extensive deep grouting at the reservoir end of the tunnel to reduce loss of water due to seepage.

### 9.3 Pattern of Holes for Grouting

For small tunnels, rings of grout holes, may be spaced at about 3 m centres, depending upon the nature of the rock. Each ring may consist of four grout holes distributed at about 90° around the periphery, with alternate rings placed vertical and 45° axes.

### APPENDIX A

**(Clause 5.2)**

**BASIC CONDITIONS FOR INCLUDING THE EFFECT OF WATER HAMMER IN THE DESIGN**

**A-1.** The basic conditions for including effect of water hammer in the design of tunnels or turbine penstock installations are divided into normal and emergency conditions with suitable factors of safety assigned to each type of operation.

**A-2. NORMAL CONDITIONS OF OPERATIONS**

**A-2.1** The basic conditions to be considered are as follows:

a) Turbine penstock installation may be operated at any head between the maximum and the minimum values of forebay water surface elevation.

b) Turbine gates may be moved at any rate of speed by action of the governor head up to a predetermined rate, or at a slower rate by manual control through the auxiliary relay valve.

c) The turbine may be operating at any gate position and be required to add or drop any or all of its load.

d) If the turbine penstock installation is equipped with any of the following pressure control devices it will be assumed that these devices are properly adjusted and function in all manner for which the equipment is designed.

1) Surge tanks,
2) Relief valves,
3) Governor control apparatus,
4) Cushioning stroke device, and
5) Any other pressure control device.

e) Unless the actual turbine characteristics are known, the effective area through the turbine gates during the maximum rate of gate movement will be taken as a linear relation with reference to time.
f) The water hammer effects shall be computed on the basis of governor head action for the governor rate which is actually set on the turbine for speed regulation. If the relay valve stops are adjusted to give a slower governor setting than that for which the governor is designed this shall be determined prior to proceeding with the design of turbine penstock installation and later adhered to at the power plant so that an economical basis for designing the penstock scroll case, etc, under normal operating conditions may be established.

g) In those instances, where due to higher reservoir elevation, it is necessary to set the stops on the main relay valve for a slower rate of gate movement, water hammer effects will be computed for this slower rate of gate movement also.

h) The reduction in head at various points along the penstock will be computed for rate of gate opening which is actually set in the governor in those cases where it appears that the profile of the penstock is unfavourable. This minimum pressure will then be used as a basis for normal design of the penstock to ensure that sub-atmospheric pressures will not cause a penstock failure due to collapse.

j) If a surge is present in the penstock system, the upsurge in the surge tank will be computed for the maximum reservoir level condition for the rejection of the turbine flow which corresponds to the rated output of the generator during the gate traversing time which is actually set on the governor.

k) The downsurge in the surge tank will be computed for minimum reservoir level condition for a load addition from speed-no-load to the full gate position during the gate traversing time which is actually set on the governor.

A-3. EMERGENCY CONDITIONS

A-3.1 The basic conditions to be considered as an emergency operation are as follows:

a) The turbine gates may be closed at any time by the action of the governor head, manual control knob with the main relay valve or the emergency solenoid device.

b) The cushioning stroke will be assumed to be inoperative.

c) If a relief valve is present, it will be assumed inoperative.

d) The gate traversing time will be taken as the minimum time for which the governor is designed.

e) The maximum head including water hammer at the turbine and along the length of the penstock will be computed for the maximum reservoir head condition for final part gate closure to the zero gate position at the maximum governor rate in \( \frac{2L}{a} \) seconds. Where \( 'L' \) is length of penstock and \( 'a' \) wave velocity.

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f) If a surge tank is present in the penstock system, the upsurge in the tank will be computed for the maximum reservoir head condition for the rejections of full gate turbine flow at the maximum rate for which the governor is designed. The downsurge in the surge tank will be computed for the minimum reservoir head condition for full gate opening from the speed-no-load position at the maximum rate for which the governor is designed. In determining the top and bottom elevations of the surge tank nothing will be added to the upsurge and down surge for this emergency condition of operation.

A-4. EMERGENCY CONDITIONS NOT TO BE CONSIDERED AS A BASIS FOR DESIGN

A-4.1 The other possible emergency conditions of operation are those during which certain pieces of control are assumed to malfunction in the most unfavourable manner. The most severe emergency head rise in a turbine penstock installation occurs from either of the two following conditions of operation:

a) Rapid closure of turbine gates in less than \( \frac{2L}{a} \) s, when the flow of water in the penstock is maximum.

b) Rhythmic opening and closing of the turbine gates when a complete cycle of gate operation is performed in \( \frac{4L}{a} \) s.

Since these conditions of operation require a complete malfunctioning of the governor control apparatus at the most unfavourable moment, the probability of obtaining this type of operation is exceedingly remote. Hence, the conditions shall not be used as a basis for design. However, after the design has been established from other considerations it is desirable that the stresses in the turbine scroll case penstock and pressure control devices be not in excess of the ultimate bursting strength or twisting strength of structures for these emergency conditions of operation.

APPENDIX B
( Clause 7.4.2.1 )

ROCK LOADS ON TUNNEL LINING

B-1. SCOPE

B-1.1 This appendix contains recommendations for evaluating rock loads on tunnel lining.
B-2. LOAD DISTRIBUTION

B-2.1 Rock load may be assumed as an equivalent uniformly distributed load over the tunnel soffit over a span equal to the tunnel width or diameter as the case may be.

B-3. LOAD

B-3.1 Rock loads may be estimated by any of the methods given in B-3.1.1 to B-3.1.3.

B-3.1.1 Rock load at depths less than or equal to $1.5 (B + H_t)$ may be taken as equal to depth of actual rock cover where $B$ is the width and $H_t$ is the height of the tunnel opening. In case of circular tunnels $B$ and $H_t$ both will be equal to the diameter of tunnel $D$.

Rock load $(H_p)$ on the roof of support in tunnel with width $B$ and height $H_t$ at depth of more than $1.5 (B + H_t)$ may be assumed to be according to Table 1.

B-3.1.2 Rock load may also be worked out using Fenner’s ellipse (see Fig. 4 on P 21) by the following equation:

$$a = \frac{b}{2} (m - 2)$$

where

- $a$ = main axis of ellipse of rock load,
- $b$ = tunnel diameter (excavated), and
- $m$ = inverse of Poisson's ratio for rock (which usually varies from 2 to 7).

The weight of rock in the shaded portion may be taken as rock load and may be considered as uniformly distributed on the diameter of tunnel.

Note — The above treatment assumes the rock to be homogeneous and to behave within elastic range. It has also limited application as it does not give any rock loads for value of Poisson's ratio equal to 0.25 and above. It does not also take into consideration the strength and characteristics of rock.

B-3.1.3 The rock load according to the Russian practice depends upon the degree of rock firmness. The rock load may be taken as that for rock area enclosed by a parabola starting from intersection points of the rupture planes with horizontal length drawn to the crown of the tunnel section. The dimensions of the parabola are given below (see Fig. 5 on P 21):

$$h = \frac{B}{2 f}$$

$$B = b + 2m \tan (45° - \phi/2)$$

where

- $\phi$ = the angle of repose of the soil,
- $f$ = the strength factor after Protodyakonov (see Table 2).

In the case of circular tunnels,

$$B = D [1 + 2 \tan (45° - \phi/2)]$$

where

$D$ = diameter of the tunnel.


<table>
<thead>
<tr>
<th>ROCK CONDITION</th>
<th>ROCK LOAD $H_p$ m</th>
<th>REMARKS</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Hard and intact</td>
<td>Zero</td>
<td>Light lining required only if spalling or popping occurs</td>
</tr>
<tr>
<td>2. Hard stratified or schisto-</td>
<td>0 to 0.50 B</td>
<td>Light support</td>
</tr>
<tr>
<td>te</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3. Massive, moderately</td>
<td>0 to 0.25 B</td>
<td>Load may change erratically from point to point</td>
</tr>
<tr>
<td>joined</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4. Moderately blocky and</td>
<td>0.25 B to 0.35 ($B + H_t$)</td>
<td>No side pressure</td>
</tr>
<tr>
<td>seamy</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5. Very blocky and seamy</td>
<td>(0.35 to 1.10) ($B + H_t$)</td>
<td>Little or no side pressure</td>
</tr>
<tr>
<td>6. Completely crushed but</td>
<td>1.10 ($B + H_t$)</td>
<td>Considerable side pressure. Softening effect of seepage towards</td>
</tr>
<tr>
<td>chemically intact</td>
<td></td>
<td>bottom of tunnel. Requires either continuous support for lower ends</td>
</tr>
<tr>
<td></td>
<td></td>
<td>of ribs or circular ribs.</td>
</tr>
<tr>
<td>7. Squeezing rock, moderate</td>
<td>(1.10 to 2.10) ($B + H_t$)</td>
<td>Heavy side pressure. Invert struts required. Circular ribs are</td>
</tr>
<tr>
<td>rate depth</td>
<td></td>
<td>recommended.</td>
</tr>
<tr>
<td>8. Squeezing rock, great</td>
<td>(2.10 to 4.50) ($B + H_t$)</td>
<td></td>
</tr>
<tr>
<td>depth</td>
<td></td>
<td></td>
</tr>
<tr>
<td>9. Swelling rock</td>
<td>Up to 80 m</td>
<td>Circular ribs required. In extreme cases use yielding support</td>
</tr>
<tr>
<td></td>
<td>irrespective</td>
<td></td>
</tr>
<tr>
<td></td>
<td>of value of ($B + H_t$)</td>
<td></td>
</tr>
</tbody>
</table>

**Note 1** — The above Table has been arrived on the basis of observation and behaviour of supports in Alpine tunnels where the load was derived mainly on loosening type of rock.

**Note 2** — The roof of the tunnel is assumed to be located below the water table. If it is located permanently above the water table, the values given for types 4 to 6 may be reduced by fifty percent.

**Note 3** — Some of the most common rock formations contain layers of shale. In an unweathered state, real shales are no worse than other stratified rocks. However, the term shale is often applied to firmly compacted clay sediments which have not yet acquired the properties of rock. Such so called shales may behave in the tunnel like squeezing or even swelling rock.

**Note 4** — If rock formation consists of sequence of horizontal layers of sandstone or lime stone and of immature shale, the excavation of the tunnel is commonly associated with a gradual compression of the rock on the both sides of the tunnel, involving a downward movement of the roof. Furthermore, the relatively low resistance against slippage at the boundaries between the so called shale and rock is likely to reduce very considerably the capacity of rock located above the roof to bridge. Hence, in such rock formations, the roof pressure may be as heavy as in a very blocky and seamy rock.
<table>
<thead>
<tr>
<th>Category</th>
<th>Strength Grade</th>
<th>Denotation of Rock (Soil)</th>
<th>Unit Weight</th>
<th>Crushing Strength</th>
<th>Strength Factor</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>Highest</td>
<td>Solid, danse quartzite, basalt and other solid rocks of exceptionally high strength.</td>
<td>2800-3000</td>
<td>2000</td>
<td>20</td>
</tr>
<tr>
<td>II</td>
<td>Very high</td>
<td>Solid, granite, quartzporphy, silica shale. Highly resistant sandstones and limestones.</td>
<td>2600-2700</td>
<td>1500</td>
<td>15</td>
</tr>
<tr>
<td>III</td>
<td>High</td>
<td>Granite and alike, very resistant sand and limestones. Quartz. Solid conglomerates.</td>
<td>2500-2600</td>
<td>1000</td>
<td>15</td>
</tr>
<tr>
<td>IIIa</td>
<td>High</td>
<td>Limestones, weathered granite. Solid sandstone, marble.</td>
<td>2500</td>
<td>800</td>
<td>8</td>
</tr>
<tr>
<td>IV</td>
<td>Moderately strong</td>
<td>Normal sandstone.</td>
<td>2400</td>
<td>600</td>
<td>6</td>
</tr>
<tr>
<td>IVa</td>
<td>Moderately strong</td>
<td>Sandstone shales.</td>
<td>2300</td>
<td>500</td>
<td>5</td>
</tr>
<tr>
<td>V</td>
<td>Medium</td>
<td>Clay-shales. Sand and Limestones of smaller resistance. Loose conglomerates.</td>
<td>2400-2600</td>
<td>400</td>
<td>4</td>
</tr>
<tr>
<td>Va</td>
<td>Medium</td>
<td>Various shales and slates. Dense marl.</td>
<td>2400-2800</td>
<td>300</td>
<td>3</td>
</tr>
<tr>
<td>VI</td>
<td>Moderately loose</td>
<td>Loose shale and very loose limestone, gypsum, frozen ground, common marl. Blocky sandstone, cemented gravel and boulders, stoney ground.</td>
<td>2200-2600</td>
<td>200-150</td>
<td>2</td>
</tr>
<tr>
<td>VIa</td>
<td>Moderately loose</td>
<td>Gravely ground. Blocky and fissured shale, compressed boulders and gravel, hard clay.</td>
<td>2200-2400</td>
<td>—</td>
<td>1.5</td>
</tr>
<tr>
<td>VII</td>
<td>Loose</td>
<td>Dense clay, Cohesive ballast. Clayey ground.</td>
<td>2000-2200</td>
<td>—</td>
<td>1.0</td>
</tr>
<tr>
<td>VIIa</td>
<td>Loose</td>
<td>Loose loam, loess, gravel.</td>
<td>1800-2000</td>
<td>—</td>
<td>0.8</td>
</tr>
<tr>
<td>VIII</td>
<td>Soils</td>
<td>Soil with vegetation peat, soft loam, wet sand.</td>
<td>1600-1800</td>
<td>—</td>
<td>0.6</td>
</tr>
<tr>
<td>IX</td>
<td>Granular soils</td>
<td>Sand, fine gravel, upfill.</td>
<td>1400-1600</td>
<td>—</td>
<td>0.5</td>
</tr>
<tr>
<td>X</td>
<td>Plastic soils</td>
<td>Silty ground, modified looses and other soils in liquid condition.</td>
<td>—</td>
<td>—</td>
<td>0.3</td>
</tr>
</tbody>
</table>
The load may be taken as uniformly distributed over the diameter of the tunnel.

Note — The above is applicable when the distance between the vertex of the pressure parabola from the bottom of the weak layer or from the ground surface is not less than \( a \). However, where this condition is not fulfilled the total value of rock load may be assumed.

\[ \text{Fig. 4 Fenner's Ellipse} \]

\[ \text{Fig. 5 Assumed Rock Load on a Circular Cavity} \]

**APPENDIX C**

( *Note Under Clause 7.4.1 and Clause 7.4.6.2*)

**FORMULAE FOR VALUES OF BENDING MOMENTS, NORMAL THRUST, RADIAL SHEAR, HORIZONTAL AND VERTICAL DEFLECTION**

C-1. The values of bending moment, normal thrust, radial shear and horizontal and vertical deflection for the loading pattern shown in Fig. 3 are given in Tables 3 to 7.

C-2. For purpose of this appendix, the following notations shall apply:

- \( E \) = Young's modulus of the lining material,
- \( I \) = moment of inertia of the section,
- \( K \) = intensity of lateral triangular load at horizontal diameter,
- \( P \) = total rock load on mean diameter,
- \( r \) = internal radius of tunnel,
- \( R \) = mean radius of tunnel lining,
- \( t \) = thickness of lining,
- \( W \) = unit weight of water,
- \( W_c \) = unit weight of concrete, and
- \( \phi \) = angle that the section makes with the vertical diameter at the centre measured from invert.
C-3. For the purpose of this appendix, the following sign conventions shall apply:

- Positive moment indicates tension on inside face and compression on outside face;
- Positive thrust means compression on the section;
- Positive shear means that considering left half of the ring the sum of all the forces on left of the section acts outwards when viewed from inside;
- Positive horizontal deflection means outward deflection with reference to centre of conduit; and
- Positive vertical deflection means downward deflection.

### TABLE 3  VALUES OF BENDING MOMENTS

(Clause C-1)

<table>
<thead>
<tr>
<th>Φ</th>
<th>Uniform Vertical Load</th>
<th>Conduit Weight</th>
<th>Contained Water</th>
<th>Lateral Pressure</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>+ 0.1250 PR</td>
<td>+ 0.4406 We t R²</td>
<td>+ 0.2203 Wr² R</td>
<td>− 0.1434 KR²</td>
</tr>
<tr>
<td>π/4</td>
<td>Zero</td>
<td>− 0.0334 We t R²</td>
<td>− 0.0167 Wr² R</td>
<td>− 0.0084 KR²</td>
</tr>
<tr>
<td>π/2</td>
<td>− 0.1250 PR</td>
<td>− 0.3927 We t R²</td>
<td>− 0.1963 Wr² R</td>
<td>+ 0.1653 KR²</td>
</tr>
<tr>
<td>3π/4</td>
<td>Zero</td>
<td>+ 0.0334 We t R²</td>
<td>+ 0.0167 Wr² R</td>
<td>− 0.0187 KR²</td>
</tr>
<tr>
<td>π</td>
<td>+ 0.1250 PR</td>
<td>+ 0.3148 We t R²</td>
<td>+ 0.1724 Wr² R</td>
<td>− 0.1295 KR²</td>
</tr>
</tbody>
</table>

### TABLE 4  VALUES OF NORMAL THRUST

(Clause C-1)

<table>
<thead>
<tr>
<th>Φ</th>
<th>Uniform Vertical Load</th>
<th>Conduit Weight</th>
<th>Contained Water</th>
<th>Lateral Pressure</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Zero</td>
<td>+ 0.1667 We t R</td>
<td>− 1.4166 Wr² R</td>
<td>+ 0.4754 KR</td>
</tr>
<tr>
<td>π/4</td>
<td>+ 0 2500 P</td>
<td>+ 1.1332 We t R</td>
<td>− 0.7869 Wr² R</td>
<td>+ 0.3058 KR</td>
</tr>
<tr>
<td>π/2</td>
<td>+ 0 500 0 P</td>
<td>+ 1.5708 We t R</td>
<td>− 0.2146 Wr² R</td>
<td>Zero</td>
</tr>
<tr>
<td>3π/4</td>
<td>+ 0 2500 P</td>
<td>+ 0.4376 We t R</td>
<td>− 0.4277 Wr² R</td>
<td>+ 0.2674 KR</td>
</tr>
<tr>
<td>π</td>
<td>Zero</td>
<td>− 0.1667 We t R</td>
<td>− 0.5834 Wr² R</td>
<td>+ 0.3782 KR</td>
</tr>
</tbody>
</table>
TABLE 5 VALUES OF RADIAL SHEAR  
(Clause C-1)

<table>
<thead>
<tr>
<th>φ</th>
<th>Uniform Vertical Load</th>
<th>Conduit Weight</th>
<th>Contained Water</th>
<th>Lateral Pressure</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
</tr>
<tr>
<td>π/4</td>
<td>-0.250 0 P</td>
<td>-0.897 6 W_e t R</td>
<td>-0.448 8 W'R'</td>
<td>+0.305 8 KR</td>
</tr>
<tr>
<td>π/2</td>
<td>Zero</td>
<td>+0.166 7 W_e t R</td>
<td>+0.083 3 W'R'</td>
<td>-0.024 6 KR</td>
</tr>
<tr>
<td>3π/4</td>
<td>+0.250 0 P</td>
<td>+0.673 2 W_e t R</td>
<td>+0.336 6 W'R'</td>
<td>-0.267 4 KR</td>
</tr>
<tr>
<td>π</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
</tr>
</tbody>
</table>

TABLE 6 VALUES OF HORIZONTAL DEFLECTION  
(Clause C-1)

<table>
<thead>
<tr>
<th>φ</th>
<th>Uniform Vertical Load</th>
<th>Conduit Weight</th>
<th>Contained Water</th>
<th>Lateral Pressure</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
</tr>
<tr>
<td>π/4</td>
<td>+0.014 73 Pr/Ed</td>
<td>+0.050 40 W_e R^4/Ed</td>
<td>+0.025 20 W'R'^3/Ed</td>
<td>-0.017 50 Kr^4/Ed</td>
</tr>
<tr>
<td>π/2</td>
<td>+0.041 67 Pr/Ed</td>
<td>+0.130 90 W_e R^4/Ed</td>
<td>+0.065 45 W'R'^3/Ed</td>
<td>-0.050 55 Kr^4/Ed</td>
</tr>
<tr>
<td>3π/4</td>
<td>+0.014 73 Pr/Ed</td>
<td>+0.042 16 W_e R^4/Ed</td>
<td>+0.021 08 W'R'^3/Ed</td>
<td>-0.016 24 Kr^4/Ed</td>
</tr>
<tr>
<td>π</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
</tr>
</tbody>
</table>

TABLE 7 VALUES OF VERTICAL DEFLECTION  
(Clause C-1)

<table>
<thead>
<tr>
<th>φ</th>
<th>Uniform Vertical Load</th>
<th>Conduit Weight</th>
<th>Contained Water</th>
<th>Lateral Pressure</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
<td>Zero</td>
</tr>
<tr>
<td>π/4</td>
<td>+0.026 94 Pr/Ed</td>
<td>+0.092 79 W_e R^4/Ed</td>
<td>+0.046 40 W'R'^3/Ed</td>
<td>-0.031 76 Kr^4/Ed</td>
</tr>
<tr>
<td>π/2</td>
<td>+0.041 67 Pr/Ed</td>
<td>+0.139 17 W_e R^4/Ed</td>
<td>+0.069 58 W'R'^3/Ed</td>
<td>-0.049 93 Kr^4/Ed</td>
</tr>
<tr>
<td>3π/4</td>
<td>+0.056 40 Pr/Ed</td>
<td>+0.185 35 W_e R^4/Ed</td>
<td>+0.092 68 W'R'^3/Ed</td>
<td>-0.068 10 Kr^4/Ed</td>
</tr>
<tr>
<td>π</td>
<td>+0.083 33 Pr/Ed</td>
<td>+0.261 80 W_e R^4/Ed</td>
<td>+0.130 90 W'R'^3/Ed</td>
<td>-0.037 39 Kr^4/Ed</td>
</tr>
</tbody>
</table>
APPENDIX D

(Clause 7.5.1)

BASIC EQUATIONS FOR ANALYSIS OF TUNNEL LINING CONSIDERING IT AND THE SURROUNDING ROCK AS A COMPOSITE CYLINDER

D-1. SCOPE

D-1.1 This appendix contains basic equations for calculating radial and tangential stresses in concrete lining and the surrounding rock mass considering both as parts of a composite cylinder.

D-2. NOTATIONS

D-2.1 For this appendix the following notations shall apply:

- \( P \) = internal hydrostatic pressure (negative compression);
- \( \sigma_t, \sigma_r, \sigma_s \) = tangential stress in rock, concrete and steel respectively;
- \( \sigma_r^*, \sigma_r, \sigma_s^* \) = radial stress in rock, concrete and steel respectively;
- \( E, E_r, E_s \) = modulus of elasticity of rock, concrete and steel respectively;
- \( m_r, m_s \) = poisson's ratio of rock, and concrete respectively;
- \( U_r, U_s, U_s^* \) = radial deformation in rock, concrete and steel respectively;
- \( x \) = radius of element;
- \( B \) & \( C \), etc = integration constants;
- \( A_r \) = areas of reinforcement per unit length of tunnel;
- \( a \) = internal diameter of the tunnel; and
- \( b \) = external diameter of the lining up to A-line.

D-3. BASIC EQUATIONS

D-3.1 Plain Cement Concrete Lining Considering that it is not Cracked

a) Basic Equations:

\[
\begin{align*}
\sigma_r &= \frac{m E}{m^2 - 1} \left[ B (m + 1) - \frac{C}{x^2} (m - 1) \right] \\
\sigma_t &= \frac{m E}{m^2 - 1} \left[ B (m + 1) + \frac{C}{x^2} (m - 1) \right] \\
U &= Bx + C/x
\end{align*}
\]
b) Limit Conditions and Constants:

1) When \( x = \infty \) \( \sigma_{r1} = 0 \)
2) When \( x = b \) \( \sigma_{r1} = \sigma_{r2} \)
3) When \( x = b \) \( \sigma_{r2} = -\rho \)
4) When \( x = b \) \( U_1 = U_2 \)

D-3.2 Plain Cement Concrete Lining Considering that it is Cracked

a) Basic Equations for Rock:

\[
\sigma_{r1} = \frac{m_1 E_1}{m_1^3 - 1} \left[ B_1 (m_1 + 1) - C_1 \frac{1}{x^2} (m_1 - 1) \right]
\]

\[
\sigma_{r2} = \frac{m_1 E_1}{m_1^3 - 1} \left[ B_1 (m_1 + 1) - C_1 \frac{1}{x^2} (m_1 - 1) \right]
\]

b) For Concrete:

\[
\sigma_{r2} = \frac{a \cdot (\sigma_{r2}) x = a}{x}
\]

\( \sigma_{t2} = 0 \) (since concrete does not take any tangential stress)

c) Limit Conditions:

1) When \( x = \infty \) \( \sigma_{r1} = 0 \)
2) When \( x = b \) \( \sigma_{r1} = \sigma_{r2} \)
3) When \( x = a \) \( \sigma_{r2} = -\rho \)

d) Constants are calculated as:

\[
B_1 = 0
\]

\[
C_1 = \frac{a \cdot b \cdot \rho (m_1 + 1)}{m_1 E_1}
\]

\( (\sigma_{r2}) x = a \), \( \sigma_{t2} = -\rho \)

D-3.3 Plain Cement Concrete Lining Considering that it is Cracked and Surrounding Rock also is Cracked for a Distance Equal to Radius Beyond which Rock is Massive and Uncracked

a) For Concrete:

\[
\sigma_{r2} = \frac{a \cdot (\sigma_{r2}) x = a}{x}
\]

\( \sigma_{t2} = 0 \)

b) For Cracked Rock:

\[
\sigma_{r1}' = \frac{a \cdot (\sigma_{r2}) x = a}{x}
\]

\( \sigma_{t1}' = 0 \)

**Note** — Symbol \( \sigma_{r1}' \) and \( \sigma_{t1}' \) refer to cracked zone of rock.
c) For Surrounding Uncracked Rock:

\[ \sigma_{r1} = \frac{m_1 E_1}{m_1^2 - 1} \left[ B_1 (m_1 + 1) - \frac{C_1}{x^2} (m_1 - 1) \right] \]

\[ \sigma_{l1} = \frac{m_1 E_1}{m_1^2 - 1} \left[ B_1 (m_1 + 1) + \frac{C_1}{x^2} (m_1 - 1) \right] \]

\[ \sigma_{r2} = \frac{m E}{m^2 - 1} \left[ B (m + 1) - \frac{C_1}{x^2} (m - 1) \right] \]

\[ \sigma_{l2} = \frac{m E}{m^2 - 1} \left[ B (m + 1) + \frac{C_1}{x^2} (m - 1) \right] \]

\[ \sigma_{r3} = \frac{E_3 A_3}{a^2} \left( B_2 a + \frac{C_2}{a} \right) \]

\[ \sigma_{l3} = \frac{E_3 A_3}{a^2} \left( B_2 a + \frac{O_2}{a} \right) \]

\[ \sigma_{r1} = \sigma_{r1}' = \sigma_{r1}'' \]

\[ \sigma_{r2} = \sigma_{r2}' = \sigma_{r2}'' = -p \]

D-3.4 Reinforced Cement Concrete Lining Considering that it is not Cracked

a) Basic Equations:

\[ \sigma_r = \frac{m E}{m^2 - 1} \left[ B (m + 1) - \frac{C_1}{x^2} (m - 1) \right] \]

\[ \sigma_l = \frac{m E}{m^2 - 1} \left[ B (m + 1) + \frac{C_1}{x^2} (m - 1) \right] \]

\[ \sigma_{z3} = \frac{E_3 A_3}{a^2} \left( B_2 a + \frac{C_2}{a} \right) \]

\[ \sigma_{z3} = \frac{E_3 A_3}{a^2} \left( B_2 a + \frac{O_2}{a} \right) \]

\[ \sigma_{r1} = \sigma_{r1}' = \sigma_{r1}'' \]

\[ \sigma_{r2} = \sigma_{r2}' = \sigma_{r2}'' = -p \]

\[ \sigma_{r3} = \sigma_{r3}' = \sigma_{r3}'' \]

b) Limit Conditions and Constants:

1) At \( r = \infty \), \( \sigma_{r1} = 0 \)

2) At \( x = b \), \( \sigma_{r1} = \sigma_{r2} \)

3) At \( x = a \), \( \sigma_{r2} = \sigma_{r3} = -p \)

4) At \( x = h \), \( \sigma_{r3} = 0 \)

\[ C_1 = B_2 b^2 + O_3 \]

\[ C_2 = \left\{ \frac{E_2 m_2 (m_1 + 1)}{E_1 m_1 (m_1 + 1)} \right\} B_2 - \left\{ \frac{E_2 m_2 (m_1 + 1)^2}{E_1 m_1 (m_2 - 1)} \right\} C_2 \]

\[ \sigma_{r3} = \frac{E_3 A_3}{a^2} \left( B_2 a + \frac{C_2}{a} \right) - \left\{ \frac{E_2 m_2}{a^2 (m_2 - 1)} + \frac{E_3 A_3}{a^3} \right\} C_2 \]

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D-3.5 Reinforced Cement Concrete Lining Considering that it is Cracked and that Because of Radial Cracks it Cannot Take Tangential Tensile Stress

Basic Equations

For rock

\[ \sigma_{t1} = \frac{E_1m_1C_1}{(m_1 + 1)^2x^2} \]
\[ \sigma_{r1} = -\sigma_{t1} \]
\[ U_1 = \frac{C_1}{x} \]

For concrete

\[ \sigma_{t1} = 0 \]
\[ \sigma_{r2} = a \left( \frac{\sigma_{r1}}{r} \right) x = \frac{a}{x} \]
\[ U_2 = \frac{a \left( \sigma_{r2} \right)}{E_2} x = \frac{a}{E_2} \log b/a \]

For Steel

\[ \sigma_{t3} = a \sigma_{r1} \]
\[ \sigma_{r3} = \frac{F_3A_3}{a^2} \left( aB_2 + C_2/a \right) \]
\[ U_3 = \frac{a^2 \sigma_{r3}}{E_3A_3} \]

Constants

\[ (\sigma_{r2}) x = a = am_1E_1E_2 + m_1E_1E_3A_s \log (b/a) + (m_1 + 1) F_2F_3A_s \]
\[ C_1 = -ab (m_1 + 1) \left( \frac{\sigma_{r2}}{m_1E_1} \right) x = a \]
\[ \sigma_{r3} = (\sigma_{r1}) x = a + \rho \]
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Headquarters:
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Fax: 91 11 3239399, 91 11 3239382

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Central : Manek Bhevan, 9 Bahadur Shah Zafar Marg, NEW DELHI 110002
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T. C. No. 14/1421, University P. O. Paayam, THIRUVANANTHAPURAM 695034
NIT Building, Second Floor, Gokulpal Market, NAGPUR 440010
Institution of Engineers (India) Building, 1332 Shivali Nagar, PUNE 411005

*Sales Office is at 5 Chowringhee Approach, P. O. Prinsep Street, CALCUTTA 700072
†Sales Office is at Noveltv Chambers, Grant Road, MUMBAI 400007
‡Sales Office is at 'F' Block, Unity Building, Narashimara Square, BANGALORE 560002

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